

Mark Scheme (Results)

Summer 2016

Pearson Edexcel International A Level in Statistics 1 (WST01/01)

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General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

PEARSON EDEXCEL IAL MATHEMATICS

General Instructions for Marking

- 1. The total number of marks for the paper is 75
- 2. The Edexcel Mathematics mark schemes use the following types of marks:
 - **M** marks: Method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
 - A marks: Accuracy marks can only be awarded if the relevant method
 (M) marks have been earned.
 - **B** marks are unconditional accuracy marks (independent of M marks)
 - Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod benefit of doubt
- ft follow through
- the symbol $\sqrt{}$ will be used for correct ft
- cao correct answer only
- cso correct solution only. There must be no errors in this part of the question to obtain this mark
- isw ignore subsequent working
- awrt answers which round to
- SC: special case
- oe or equivalent (and appropriate)
- d... or dep dependent
- indep independent
- dp decimal places
- sf significant figures
- * The answer is printed on the paper or ag- answer given
- L or d... The second mark is dependent on gaining the first mark
- 4. All A marks are 'correct answer only' (cao.), unless shown, for example, as A1 ft to indicate that previous wrong working is to be followed through. After a misread however, the subsequent A marks affected are treated as A ft, but manifestly absurd answers should never be awarded A marks.

- 5. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
- 6. If a candidate makes more than one attempt at any question:
 - If all but one attempt is crossed out, mark the attempt which is NOT crossed out.
 - If either all attempts are crossed out or none are crossed out, mark all the attempts and score the highest single attempt.
- 7. Ignore wrong working or incorrect statements following a correct answer.

Question	C. I.	Marks	
Number	Scheme		
1.			
(a)	$S_{ww} = 41252 - \frac{640^2}{10} = \frac{292}{10}$	M1A1	
	$S_{wp} = 27557.8 - \frac{640 \times 431}{10} = -26.2$	A1	
(b)	$r = \frac{-26.2}{\sqrt{292 \times 2.72}}$	(3)	
		M1	
	=-0.9297 awrt -0.930	A1 (2)	
(c)	As <u>weight</u> increases the percentage of <u>oil</u> content decreases o.e.	B1 (1)	
(d)	$b = \frac{-26.2}{292} = -0.0897$ awrt $\underline{-0.09}$	M1 A1	
	$a = \frac{431}{10} - \left(\frac{-26.2}{292}\right) \times \left(\frac{640}{10}\right) = 48.842$	M1	
	p = 48.8 - 0.0897w	A1 (4)	
(e)	$p = 48.8 - 0.0897 \times 60$	M1	
	= 43.4/43.5 awrt <u>43.4/43.5</u>	A1	
		(2) Total 12	
	Notes		
(a)	M1 for a correct expression for S_{ww} or S_{wp} (may be implied by one correct a 1 st A1 for either $S_{ww} = 292$ or $S_{wp} = -26.2$ 2 nd A1 for both $S_{ww} = 292$ and $S_{wp} = -26.2$	inswer)	
(b)	M1 for a correct expression (Allow ft of their S_{ww} or S_{wp} provided $S_{ww} \neq 41252$ and $S_{wp} \neq 27557.8$). Condone missing "—" A1 for awrt –0.930 (Condone –0.93 for M1A1 if correct expression is seen) (Answer only awrt –0.930 scores 2/2 but answer only –0.93 is M1A0)		
(c)	B1 For a correct contextual description of negative correlation which must include weight and oil (but w increases as p decreases is not sufficient)		
(d)	1 st M1 for a correct expression for b (Allow ft) 1 st A1 for awrt -0.09 2 nd M1 for a correct method for a ft their value of b (Allow $a = 43.1 + b \times 6$ 2 nd A1 for a correct equation for p and w with $a = $ awrt 48.8 and $b = $ awrt -1 0. No fractions. Equation in x and y is A0	54) 0.0897	
(e)	M1 substituting $w = 60$ into their equation A1 awrt 43.4 or 43.5 (Answer only scores 2/2)		

Question	Cahama	Montro
Number	Scheme	Marks
2.	$1.5 \times 12 = 18$ 20 people represented by 18 (cm ²) or 1 person is represented by 0.9 (cm ²)	M1
	20×94.5	M1
	$x = \frac{20 \times 94.5}{18} \text{ oe}$	
	= 105 (people)	A1cao (3)
		Total 3
	Notes	200020
	1^{st} M1 for an attempt to relate area to frequency (e.g. $\frac{20}{18}$ or $\frac{18}{20}$ seen)	
	2^{nd} M1 for a correct expression/equation for total frequency e.g. $\frac{18}{20} = \frac{94.5}{x}$ A1 for 105cao	

Scheme	Ma	rks	
(Discrete) <u>Uniform</u>	B1		
1		(1)	
$P(X = 4) = \frac{1}{5}$ oe	B1		
2		(1)	
$F(3) = \frac{3}{5} \text{ oe}$	B1		
_	3.51	(1)	
$=\frac{-}{5}$ oe	Al		
E(X) = 3		(2)	
	B1	(1)	
$E(\mathbf{Y}^2) = \frac{1}{2} \left(1^2 + 2^2 + 3^2 + 4^2 + 5^2 \right)$	у л 1	(1)	
= <u>11</u>	AI	(2)	
Var $(X) = 11 - 3^2$ or $\frac{(5+1)(5-1)}{12}$	M1		
12			
= <u>2</u>	Al	(2)	
11.4 = aE(X) - 3 or $11.4 = 3a - 3$	M1		
= 46.08 awrt <u>46.1</u>	A1		
	T D. 4	(4)	
Notes	Tot	<u>al 14</u>	
B1 for uniform			
M1 for identifying the correct probabilities i.e. $P(X > 3.5)$ or $P(X = 4) + P(X = 4)$	(X=5)		
M1 for a correct expression			
	1)		
M1 for either 'their (f)' – 'their (e)' $\frac{1}{2}$ or for a correct expression $\frac{(5+1)(5-1)}{12}$	<u>1)</u>		
1 st M1 for setting up a correct linear equation using $aE(X) - 3 = 11.4$			
by a correct answer or correct ft answer) NB 'their $Var(X)$ ' < 0 is M0 has			
	(Discrete) Uniform $P(X = 4) = \frac{1}{5} \text{ oc}$ $F(3) = \frac{3}{5} \text{ oe}$ $P(3X - 3 > X + 4) = P(X > 3.5)$ $= \frac{2}{5} \text{ oe}$ $E(X) = \frac{3}{5}$ $E(X) = \frac{3}{5}$ $E(X^2) = \frac{1}{5} (1^2 + 2^2 + 3^2 + 4^2 + 5^2)$ $= \frac{11}{12}$ $= \frac{2}{5}$ $11.4 = aE(X) - 3 \text{ or } 11.4 = 3a - 3$ $a = 4.8$ $Var(4.8X - 3) = 4.8 \cdot 2 \cdot $	(Discrete) <u>Uniform</u> $P(X = 4) = \frac{1}{5} \text{ oe}$ $F(3) = \frac{3}{5} \text{ oe}$ $P(3X - 3 > X + 4) = P(X > 3.5)$ $= \frac{2}{5} \text{ oe}$ $E(X) = \frac{3}{5}$ $E(X) = \frac{3}{5} \text{ oe}$ $E(X) = \frac{3}{5} \text{ oe}$ $E(X) = \frac{3}{5} \text{ or}$ $E(X) $	

4.(a) (b) (c)	7.5 <u>and</u> 25 Mean = 10.3125 $\sigma = \sqrt{\frac{120125}{80}} - 10.3125^{2}$ = 6.6188 (s = 6.6605) awrt <u>6.62</u>	B1 (1) B1 (1) M1	
, ,	$\sigma = \sqrt{\frac{120125}{80} - 10.3125^2}$	B1 (1)	
(c)		M1	
	= 6.6188 (s = 6.6605) awrt 6.62		
	<u> </u>	A1 (2)	
(d)	Median = $\{5\} + \frac{20}{24} \times 5$ or $\{10\} - \frac{4}{24} \times 5$	M1	
	= 9.16666 awrt 9.17	A1 (2)	
(e)	Mean > median ∴ positive skew	$M1A1 \tag{2}$	
(f)	t = 10v + 5		
	Mean = $10 \times 10.3125 + 5$ = 108.125 awrt 108	M1 A1	
	$=108.125$ awrt $\underline{108}$ $\sigma = 10 \times 6.6188$	M1	
	= 66.188 (66.605 from s) awrt <u>66.2</u>		
		(4)	
	N T (Total 12	
(a)	Notes B1 both values correct (may be seen in table)		
(a) (b)	B1 for awrt 10.3 (Do not allow improper fractions).		
(c)	M1 for a correct expression including the square root (allow ft from their mean) A1 for awrt 6.62 (Allow $s = \text{awrt } 6.66$)		
(d)	M1 for a correct fraction: $\frac{20}{24} \times 5$ or if using $n + 1$ for $\frac{20.5}{24} \times 5$		
	may be scored from working down $-\frac{4}{24} \times 5$		
	A1 for awrt 9.17 or (if using $n + 1$) for awrt 9.27		
(e)	M1 for a correct comparison of 'their b' and 'their d' (must have an answer to both (b) and (d)) Comparison may be part of bigger expression e.g. $3(\text{mean} - \text{median})/\text{s.d.}$ Allow use of $Q_3 - Q_2 > Q_2 - Q_1$ only if $Q_1 = 5$ and $Q_3 = 15$ are both seen		
	A1 for positive skew (which must follow from their values)		
(f)	1^{st} M1 for $10\times$ "their mean"+5 2^{nd} M1 for $10\times$ "their sd"		
	Use of decoded data to find mean must be fully correct i.e. \$650/\$0 = asset 10\$	(M1A1)	
	Use of decoded data to find mean must be fully correct, i.e. $8650/80 = \text{awrt } 108 \text{ (M1)}$ Use of decoded data to find s.d. must be fully correct, i.e. $\sqrt{\frac{1285750}{80} - \left(\frac{8650}{80}\right)^2} = \text{awrt } 66$		

Question Number	Scheme	Marks
5. (a)	$P(T=2) = 3 \times \frac{1}{6} \times \frac{1}{6} = \frac{1}{12}$ oe	M1 A1 (2)
(b)	P(T=3) = [P(0,3) + P(1,2) + P(2,1)] + P(3)	
	$= \left(\frac{1}{6} \times \frac{1}{2}\right) + \left(\frac{1}{6} \times \frac{1}{6}\right) + \left(\frac{1}{6} \times \frac{1}{6}\right) + \frac{1}{2}$	M1M1
	$=\frac{23}{36} \text{ oe}$	A1 (3)
(c)	$P(T = 3 \text{rolled twice}) = \frac{P((T = 3) \cap \text{die rolled twice})}{P(\text{die rolled twice})}$	M1
	$= \frac{\frac{5}{36}}{\frac{1}{2}}$ $= \frac{5}{18} \text{ oe}$	M1
	$=\frac{5}{18}$ oe	A1 (3)
		Total 8
	Notes	
	Correct answer only in (a), (b) or (c) scores full marks for that part.	
(a)	Methods leading to answers > 1 score 0 marks M1 for a correct expression A1 allow exact equivalent $(\frac{1}{6} \times \frac{1}{2} = \frac{1}{12} \text{ is M0A0}).$	
(b)	1^{st} M1 for $\frac{1}{2}$ + at least one correct product	
	2 nd M1 for fully correct expression A1 allow exact equivalent	
(c)	1^{st} M1 for correct conditional probability ratio (this mark may be implied by but going on to assume independence [using numerator P($T = 3$) × P(rolled M0M0A0.	
	2 nd M1 for a correct numerical ratio of probabilities (allow ft of (their (b) –	$(\frac{1}{2})$ as
	numerator) A1 allow exact equivalent	

Question Number	Scheme		Marks
6. (a)	$[P(A \cup C) =] \frac{9}{10} \text{ oe}$		B1
(b)	$P(A \cup B) = P(A) + P(B) - P(A) \times P(B)$		(1) M1
	$\frac{5}{8} = \frac{2}{5} + P(B) - \frac{2}{5}P(B)$		M1 A1
	$P(B) = \frac{3}{8} *$		A1cso
(c)	$[P(A B) = P(A) =] \frac{2}{5} \text{ oe}$		(4) B1
		_	(1)
(d)	$A \longrightarrow B$	Diagram	B1
	$\begin{array}{c c} & & & \\ \hline & 0.25 & \hline & 0.15 & \underline{0.05} \end{array}$	0.15 <u>and</u> 0.25	M1
	0 0.175	0.05 <u>and</u> <u>0.05</u>	M1
	0.325 C 0.05	0.175 <u>and</u> 0.325	M1 A1
			(5) Total 11
(b)	Notes $1^{\text{st}} \text{ M1 for use of } P(A \cup B) = P(A) + P(B) - P(A)$	$\cap B$)	
(6)	2^{nd} M1 for use of $P(A \cap B) = P(A) \times P(B)$ (But just	, and the second	is M0M0)
A=1	1 st A1 a correct equation 2 nd A1 cso (No wrong working seen dependent on a (allow a full verification method, however, substitut the other P(B) (e.g. using 3/20 to find 3/8) can score B1 3 circles intersecting, see diagram above, (at lea	Il previous marks) ion of P(B)=3/8 into only one M1M0A0A0) ast 2 labelled) with the two zero	P(B) to find
(d)	A does not intersect C (Do not allow blank spaces for $\underline{\mathbf{or}}$ 3 circles, see diagram below, (at least 2 labelled) do not intersect 1^{st} M1 0.15 placed in $(A \cap B \cap C')$ and 0.25 place	where B intersects A and C but $A \cap B' \cap C'$	t A and C
	2^{nd} M1 0.3 – 'their 0.25' <u>and</u> 1 – ('their 0.15' + 'their ord 1.5')	-	
	$3^{\text{rd}} \text{ M1 } \frac{3}{8}$ - ("their 0.15" + "their <u>0.05"</u>), i.e. P(B) =	-	
	For the 3^{rd} M mark, blank regions inside P(B) and P(A1 fully correct with box A $\frac{2}{40}$	(C) are not treated as 0s and so	ore M0
	10 6 2	7 13	

Question Number	Scheme		Mark	ΚS
7(a)(i)	$P(X > 505) = P\left(Z > \frac{505 - 503}{1.6}\right)$ $= 1 - P(Z < 1.25) = 1 - 0.8944$ $= 0.1056$	overt 0 106	M1 M1 A1	
(ii)	$P(501 < X < 505) = 1 - 2 \times 0.1056 \text{or} 0.8944 - 0.1056$ $= 0.7888$	awrt <u>0.106</u> awrt <u>0.789</u>	M1 A1	(3)
(b)	$P(X \le w) = 0.9713$ or $P(X \ge w) = 0.0287$ (may be implied by $z = \pm 1$)	1.9)	M1	(2)
	$\frac{w-503}{1.6} = 1.9 \qquad \text{or} \frac{(1006-w)-503}{1.6} = -1.9$ $w = 506.04$	awrt <u>506</u>	M1 A1	(3)
(c)	$\frac{r-503}{q} = -2.3263$ $\frac{r+6-503}{q} = 1.6449$		M1A1	(3)
	$ \begin{array}{l} 1.6449q - 6 = -2.3263q \\ q = 1.51 \\ r = 499.48 \end{array} $	awrt <u>1.51</u> awrt <u>499</u>	ddM1 A1 A1	(7)
	N .		Total	. ,
(a)(i)	Notes 1st M1 standardising with 505, 503 and 1.6. May be implied by use of	of 1 25 (Allow	+)	
(u)(1)	2^{nd} M1 for $1 - P(Z \le 1.25)$ i.e. a correct method for finding $P(Z \ge 1.65)$ e.g. $1 - p$ where $0.5 \le p \le 0.99$, 	
(ii)	$M1 1 - 2 \times their(i)$			
(b)	1 st M1 for using symmetry to find the area of one tail (may be seen in a diagram) 2^{nd} M1 a single standardisation with 503, 1.6 and w (or $1006 - w$) and set = $\pm z$ value (1.8 < $ z $ < 2) A1 for awrt 506 which must come from correct working. (Answer only : 506 scores 0/3, but 506.0with no working send to review)			
(c)	$1^{\text{st}} \text{ M1 } \frac{r - 503}{q} = z \text{ value where } z > 2$ $1^{\text{st}} \text{ A1 } \frac{r - 503}{q} = \text{awrt } -2.3263 \text{ (signs must be compatible)}$ $2^{\text{nd}} \text{ M1 } \frac{r + 6 - 503}{q} = z \text{ value where } z > 1$			
	2^{nd} A1 $\frac{r+6-503}{q} = \text{awrt } 1.6449 \text{ (signs must be compatible)}$ Special Case: Less than 4dp z-values: use of awrt 2.32/2.33/2.34 and score M1 A0 M1 and then A1 provided both equations have compat $3^{\text{rd}} \text{ M1 (dep on both Ms)}$ attempt to solve simultaneous equations lea 3^{rd}A1 for awrt 1.51 4^{th}A1 for awrt 499 (allow 499.5)	ible signs.		



